#### Machine Learning for Text

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Quants 3: Quantitative Text Analysis

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# Outline

- Supervised learning overview
- Creating a labeled set and evaluating its reliability
- Classifier performance metrics
- Types of classifiers:
  - Naive Bayes
  - Regularized regression
  - Support Vector Machines (SVMs)
  - Ensemble classifiers
- From classification to scaling
  - Basics of supervised scaling methods
  - Wordscores
  - Practical aspects
  - From supervised learning to supervised scaling
  - Examples

# Supervised machine learning

Goal: classify documents into pre existing categories.

e.g. authors of documents, sentiment of tweets, ideological position of parties based on manifestos, tone of movie reviews...

#### What we need:

- Hand-coded dataset (labeled), to be split into:
  - Training set: used to train the classifier
  - Validation/Test set: used to validate the classifier
- Method to extrapolate from hand coding to unlabeled documents (classifier):
  - Naive Bayes, regularized regression, SVM, K-nearest neighbors, ensemble methods...
- Approach to validate classifier: cross-validation
- Performance metric to choose best classifier and avoid overfitting: confusion matrix, accuracy, precision, recall...

# Classification v. scaling methods compared

- Machine learning focuses on identifying classes (classification), while social science is typically interested in locating things on latent traits (scaling)
- But the two methods overlap and can be adapted will demonstrate later using the Naive Bayes classifier
- Applying lessons from machine learning to supervised scaling, we can
  - Apply classification methods to scaling
  - Improve it using lessons from machine learning

## Supervised v. unsupervised methods compared

- The goal (in text analysis) is to differentiate *documents* from one another, treating them as "bags of words"
- Different approaches:
  - Supervised methods require a training set that exemplify contrasting classes, identified by the researcher
  - Unsupervised methods scale documents based on patterns of similarity from the term-document matrix, without requiring a training step
- Relative advantage of supervised methods:

You already know the dimension being scaled, because you set it in the training stage

Relative disadvantage of supervised methods:

You *must* already know the dimension being scaled, because you have to feed it good sample documents in the training stage

Supervised v. unsupervised methods: Examples

#### General examples:

- Supervised: Naive Bayes, regularized regression, Support Vector Machines (SVM)
- Unsupervised: topic models, IRT models, correspondence analysis, factor analytic approaches
- Political science applications
  - Supervised: Wordscores (LBG 2003); SVMs (Yu, Kaufman and Diermeier 2008); Naive Bayes (Evans et al 2007)
  - Unsupervised: Structural topic model (Roberts et al 2014);
    "Wordfish" (Slapin and Proksch 2008); two-dimensional IRT (Monroe and Maeda 2004)

Supervised learning v. dictionary methods

- Dictionary methods:
  - Advantage: not corpus-specific, cost to apply to a new corpus is trivial
  - Disadvantage: not corpus-specific, so performance on a new corpus is unknown (domain shift)
- Supervised learning can be conceptualized as a generalization of dictionary methods, where features associated with each categories (and their relative weight) are learned from the data
- By construction, they will outperform dictionary methods in classification tasks, as long as training sample is large enough

## Creating a labeled set

How do we obtain a labeled set?

- External sources of annotation
  - Disputed authorship of Federalist papers estimated based on known authors of other documents
  - Party labels for election manifestos
  - Legislative proposals by think tanks (text reuse)

#### Expert annotation

- "Canonical" dataset in Comparative Manifesto Project
- In most projects, undergraduate students (expertise comes from training)
- Crowd-sourced coding
  - Wisdom of crowds: aggregated judgments of non-experts converge to judgments of experts at much lower cost (Benoit et al, 2016)
  - Easy to implement with CrowdFlower or MTurk

#### Code the Content of a Sample of Tweets

Instructions -

In this job, you will be presented with tweets about the recent protests related to race and law enforcement in the U.S.

You will have to read the tweet and answer a set of questions about its content.

Read the tweet below paying close attention to detail:

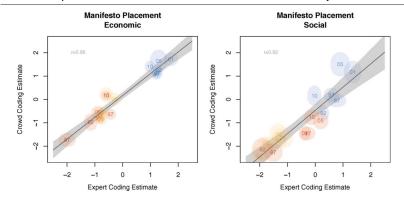
Tweet ID: 447



Is this tweet related to the ongoing debate about law enforcement and race in the United States?

- ⊖ Yes
- O No
- O Don't Know

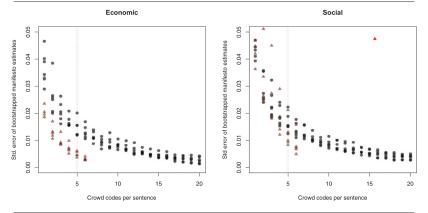
#### Crowd-sourced text analysis (Benoit et al, 2016 APSR)



#### FIGURE 3. Expert and Crowd-sourced Estimates of Economic and Social Policy Positions

## Crowd-sourced text analysis (Benoit et al, 2016 APSR)





Note: Each point is the bootstrapped standard deviation of the mean of means aggregate manifesto scores, computed from sentencelevel random n subsamples from the codes.

Evaluating the quality of a labeled set

Any labeled set should be tested and reported for its inter-rate reliability, at three different standards:

Туре	Test Design	Causes of Disagreements	Strength
Stability	test-retest	intraobserver inconsistencies	weakest
Reproduc- ibility	test-test	intraobserver inconsistencies + interobserver disagreements	medium
Accuracy	test-standard	intraobserver inconsistencies + interobserver disagreements + deviations from a standard	strongest

## Measures of agreement

Percent agreement Very simple:

(number of agreeing ratings) / (total ratings) \* 100%

Correlation

- (usually) Pearson's r, aka product-moment correlation
- ► Formula:  $r_{AB} = \frac{1}{n-1} \sum_{i=1}^{n} \left( \frac{A_i \bar{A}}{s_A} \right) \left( \frac{B_i \bar{B}}{s_B} \right)$
- May also be ordinal, such as Spearman's rho or Kendall's tau-b
- Range is [0,1]
- Agreement measures
  - Take into account not only observed agreement, but also agreement that would have occured by chance
  - Cohen's  $\kappa$  is most common
  - Krippendorf's  $\alpha$  is a generalization of Cohen's  $\kappa$
  - Both range from [0,1]

# Reliability data matrixes

Example here used binary data (from Krippendorff)

Article:	1	2	3	4	5	6	7	8	9	10	
Coder A	1	1	0	0	0	0	0	0	0	0	
Coder B	0	1	1	0	0	1	0	1	0	0	

- ▶ A and B agree on 60% of the articles: 60% agreement
- Correlation is (approximately) 0.10
- Observed disagreement: 4
- Expected *dis*agreement (by chance): 4.4211
- Krippendorff's  $\alpha = 1 \frac{D_o}{D_e} = 1 \frac{4}{4.4211} = 0.095$
- Cohen's  $\kappa$  (nearly) identical

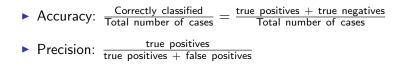
## Basic principles of supervised learning

- Generalization: A classifier or a regression algorithm learns to correctly predict output from given inputs not only in previously seen samples but also in previously unseen samples
- Overfitting: A classifier or a regression algorithm learns to correctly predict output from given inputs in previously seen samples but fails to do so in previously unseen samples. This causes poor prediction/generalization.
- Goal is to maximize the frontier of precise identification of true condition with accurate recall

# Performance metrics

Confusion matrix:

	ľ	True condition			
		Positive	Negative		
Prediction	Positive	True Positive	ve False Positive (Type I error)		
	Negative	False Negative (Type II error)	True Negative		Prediction



# Example: measuring performance

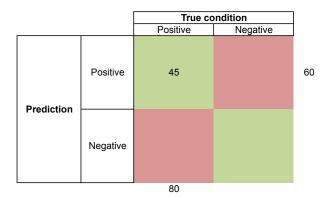
Assume:

- We have a corpus where 80 documents are really positive (as opposed to negative, as in sentiment)
- Our method declares that 60 are positive
- ▶ Of the 60 declared positive, 45 are actually positive

Solution:

$$\begin{aligned} \text{Precision} &= (45/(45+15)) = 45/60 = 0.75\\ \text{Recall} &= (45/(45+35)) = 45/80 = 0.56 \end{aligned}$$

## Accuracy?



#### add in the cells we can compute

		True condition			
		Positive	Negative		
Prediction	Positive	45	15	60	
	Negative	35			

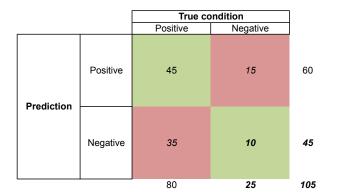
80

# but need True Negatives and N to compute accuracy

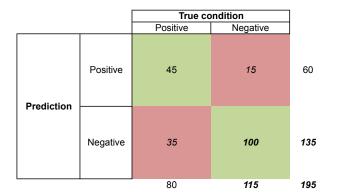
		ondition	]	
		Positive	Negative	
Prodiction	Positive	45	15	60
Prediction	Negative	35	???	

80

## assume 10 True Negatives:

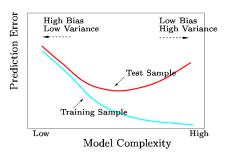


#### now assume 100 True Negatives:



# Measuring performance

- Classifier is trained to maximize in-sample performance
- But generally we want to apply method to new data
- Danger: overfitting



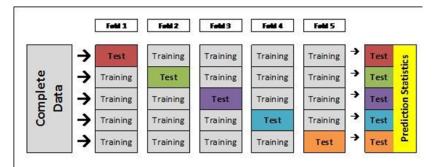
- Model is too complex, describes noise rather than signal (Bias-Variance trade-off)
- Focus on features that perform well in labeled data but may not generalize (e.g. "inflation" in 1980s)
- In-sample performance better than out-of-sample performance

- Solutions?
  - Randomly split dataset into training and test set
  - Cross-validation

# **Cross-validation**

Intuition:

- Create K training and test sets ("folds") within training set.
- For each k in K, run classifier and estimate performance in test set within fold.
- Choose best classifier based on cross-validated performance



Example: Theocharis et al (2016 JOC)

Why do politicians not take full advantage of interactive affordances of social media?

A politician's incentive structure

 $\begin{array}{l} \mathsf{Democracy} \to \mathsf{Dialogue} > \mathsf{Mobilisation} > \mathsf{Marketing} \\ \mathsf{Politician} \to \mathsf{Marketing} > \mathsf{Mobilisation} > \mathsf{Dialogue^*} \end{array}$ 

- H1: Politicians make broadcasting rather than engaging use of Twitter
- H2: Engaging style of tweeting is positively related to impolite or uncivil responses

#### Data collection and case selection

Data: European Election Study 2014, Social Media Study

- List of all candidates with Twitter accounts in 28 EU countries
  - 2,482 out of 15,527 identified MEP candidates (16%)
- Collaboration with TNS Opinion to collect all tweets by candidates and tweets mentioning candidates (tweets, retweets, @-replies), May 5th to June 1st 2014.

Case selection: expected variation in politeness/civility

	Received bailout	Did not receive bailout
High support for EU	Spain (55.4%)	Germany (68.5%)
Low support for EU	Greece (43.8%)	UK (41.4%)
/ A /		

(% indicate proportion of country that considers the EU to be "a good thing")

Data collection and case selection

#### Data coverage by country

Country	Lists	Candidates	on Twitter	Tweets
Germany	9	501	123 (25%)	86,777
Greece	9	359	99 (28%)	18,709
Spain	11	648	221 (34%)	463,937
UK	28	733	304 (41%)	273,886

## Coding tweets

Coded data: random sample of  ${\sim}7{,}000$  tweets from each country, labeled by undergraduate students:

#### 1. Politeness

- Polite: tweet adheres to politeness standards.
- Impolite: ill-mannered, disrespectful, offensive language...

#### 2. Communication style

- Broadcasting: statement, expression of opinion
- Engaging: directed to someone else/another user

#### 3. Political content: moral and democracy

Tweets make reference to: freedom and human rights, traditional morality, law and order, social harmony, democracy...

**Incivility** = impoliteness + moral and democracy

# Coding tweets

Coding process: summary statistics					
	Germany	Greece	Spain	UK	
Coded by 1/by 2	2947/2819	2787/2955	3490/1952	3189/3296	
Total coded	5766	5742	5442	6485	
Impolite	399	1050	121	328	
Polite	5367	4692	5321	6157	
% Agreement	92	80	93	95	
Krippendorf/Maxwell	0.30/0.85	0.26/0.60	0.17/0.87	0.54/0.90	
Broadcasting	2755	2883	1771	1557	
Engaging	3011	2859	3671	4928	
% Agreement	79	85	84	85	
Krippendorf/Maxwell	0.58/0.59	0.70/0.70	0.66/0.69	0.62/0.70	
Moral/Dem.	265	204	437	531	
Other	5501	5538	5005	5954	
% Agreement	95	97	96	90	
Krippendorf/Maxwell	0.50/0.91	0.53/0.93	0.41/0.92	0.39/0.81	

## Machine learning classification of tweets

Coded tweets as training dataset for a machine learning classifier:

- Text preprocessing: lowercase, remove stopwords and punctuation (except # and @), transliterating to ASCII, stem, tokenize into unigrams and bigrams. Keep tokens in 2+ tweets but <90%.</li>
- 2. Train classifier: logistic regression with L2 regularization (ridge regression), one per language and variable
- 3. Evaluate classifier: compute accuracy using 5-fold crossvalidation

# Machine learning classification of tweets

#### Classifier performance (5-fold cross-validation)

	ŮK	Spain	Greece	Germany
Accuracy	0.821	0.775	0.863	0.806
Precision	0.837	0.795	0.838	0.818
Recall	0.946	0.890	0.894	0.832
Accuracy	0.954	0.976	0.821	0.935
Precision	0.955	0.977	0.849	0.938
Recall	0.998	1.000	0.953	0.997
Accuracy	0.895	0.913	0.957	0.922
Precision	0.734	0.665	0.851	0.770
Recall	0.206	0.166	0.080	0.061
	Precision Recall Accuracy Precision Recall Accuracy Precision	Accuracy0.821Precision0.837Recall0.946Accuracy0.954Precision0.955Recall0.998Accuracy0.895Precision0.734	Accuracy0.8210.775Precision0.8370.795Recall0.9460.890Accuracy0.9540.976Precision0.9550.977Recall0.9981.000Accuracy0.8950.913Precision0.7340.665	Accuracy0.8210.7750.863Precision0.8370.7950.838Recall0.9460.8900.894Accuracy0.9540.9760.821Precision0.9550.9770.849Recall0.9981.0000.953Accuracy0.8950.9130.957Precision0.7340.6650.851

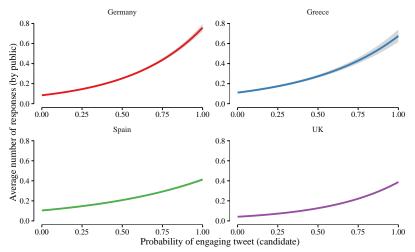
#### Top predictive n-grams

Broadcasting	just, hack, #votegreen2014, :, and, @ ', tonight, candid,
	up, tonbridg, vote @, im @, follow ukip, ukip @, $\#$ telleu-
	rop, angri, $\#$ ep2014, password, stori, $\#$ vote2014, team,
	#labourdoorstep, crimin, bbc news
Engaging	@ thank, @ ye, you'r, @ it', @ mani, @ pleas, u, @ hi, @ con-
	gratul, :), index, vote $\#$ skip, $@$ good, fear, cheer, haven't,
	lol, @ i'v, you'v, @ that', choice, @ wa, @ who, @ hope
Impolite	cunt, fuck, twat, stupid, shit, dick, tit, wanker, scumbag,
	moron, cock, foot, racist, fascist, sicken, fart, @ fuck, ars,
	suck, nigga, nigga ?, smug, idiot, @arsehol, arsehol
Polite	@ thank, eu, $#$ ep2014, thank, know, candid, veri, politi-
	cian, today, way, differ, europ, democraci, interview, time,
	tonight, @ think, news, european, sorri, congratul, good, :,
	democrat, seat
Moral/Dem.	democraci, polic, freedom, media, racist, gay, peac, fraud,
	discrimin, homosexu, muslim, equal, right, crime, law, vi-
	olenc, constitut, faith, bbc, christian, marriag, god, cp,
	racism, sexist
Others	@ ha, 2, snp, nice, tell, eu, congratul, campaign, leav, al-
	readi, wonder, vote @, ;), hust, nh, brit, tori, deliv, bad,
	immigr, #ukip, live, count, got, roma

-

## Predictive validity

Citizens are more likely to respond to candidates when they adopt an engaging style

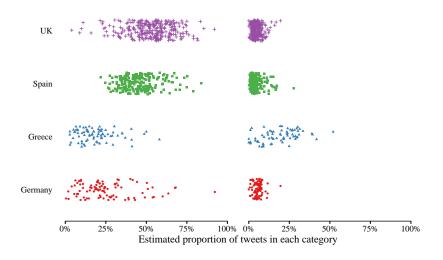


# Results: H1

#### Proportion of engaging tweets sent and impolite tweets received, by candidate and country

Engaging (based on candidates)

Impolite (based on public)



#### Results: H2

Is engaging style positively related to impolite responses?

Three levels of analysis:

- 1. Across candidates: candidates who send more engaging tweets receive more impolite responses.
- 2. Within candidates, over time: the number of impolite responses increases during the campaign for candidates who send more engaging tweets
- 3. Across tweets: tweets that are classified as engaging tend to receive more impolite responses

# Types of classifiers

General thoughts:

- Trade-off between accuracy and interpretability
- Parameters need to be cross-validated

Frequently used classifiers:

- Naive Bayes
- Regularized regression
- SVM
- Others: k-nearest neighbors, tree-based methods, etc.
- Ensemble methods

Multinomial Bayes model of Class given a Word

Consider J word types distributed across N documents, each assigned one of K classes.

At the word level, Bayes Theorem tells us that:

$$P(c_k|w_j) = \frac{P(w_j|c_k)P(c_k)}{P(w_j)}$$

For two classes, this can be expressed as

$$= \frac{P(w_{j}|c_{k})P(c_{k})}{P(w_{j}|c_{k})P(c_{k}) + P(w_{j}|c_{\neg k})P(c_{\neg k})}$$
(1)

Multinomial Bayes model of Class given a Word Class-conditional word likelihoods

$$P(c_k|w_j) = \frac{P(w_j|c_k)P(c_k)}{P(w_j|c_k)P(c_k) + P(w_j|c_{\neg k})P(c_{\neg k})}$$

- The word likelihood within class
- The maximum likelihood estimate is simply the proportion of times that word j occurs in class k, but it is more common to use Laplace smoothing by adding 1 to each observed count within class

# Multinomial Bayes model of Class given a Word Word probabilities

$$P(c_k|w_j) = \frac{P(w_j|c_k)P(c_k)}{P(w_j)}$$

- This represents the word probability from the training corpus
- Usually uninteresting, since it is constant for the training data, but needed to compute posteriors on a probability scale

Multinomial Bayes model of Class given a Word Class prior probabilities

$$P(c_k|w_j) = \frac{P(w_j|c_k)P(c_k)}{P(w_j|c_k)P(c_k) + P(w_j|c_{\neg k})P(c_{\neg k})}$$

- This represents the class prior probability
- Machine learning typically takes this as the document frequency in the training set

Multinomial Bayes model of Class given a Word Class posterior probabilities

$$P(c_k|w_j) = \frac{P(w_j|c_k)P(c_k)}{P(w_j|c_k)P(c_k) + P(w_j|c_{\neg k})P(c_{\neg k})}$$

- This represents the posterior probability of membership in class k for word j
- Key for the classifier: in new documents, we only observe word distributions and want to predict class

#### Moving to the document level

The "Naive" Bayes model of a joint document-level class posterior assumes conditional independence, to multiply the word likelihoods from a "test" document, to produce:

$$P(c|d) = P(c) \prod_{j} \frac{P(w_{j}|c)}{P(w_{j})}$$
  
 $P(c|d) \propto P(c) \prod_{j} P(w_{j}|c)$ 

This is why we call it "naive": because it (wrongly) assumes:

- conditional independence of word counts
- positional independence of word counts

#### Naive Bayes Classification Example

## (From Manning, Raghavan and Schütze, *Introduction to Information Retrieval*)

► Table 13.1	Data for parameter estimation examples.		
	docID	words in document	in $c = China$ ?
training set	1	Chinese Beijing Chinese	yes
	2	Chinese Chinese Shanghai	yes
	3	Chinese Macao	yes
	4	Tokyo Japan Chinese	no
test set	5	Chinese Chinese Chinese Tokyo Japan	?

#### Naive Bayes Classification Example

**Example 13.1:** For the example in Table 13.1, the multinomial parameters we need to classify the test document are the priors  $\hat{P}(c) = 3/4$  and  $\hat{P}(\overline{c}) = 1/4$  and the following conditional probabilities:

$$\begin{array}{rcl} \hat{P}({\sf Chinese}|c) &=& (5+1)/(8+6) = 6/14 = 3/7\\ \hat{P}({\sf Tokyo}|c) = \hat{P}({\sf Japan}|c) &=& (0+1)/(8+6) = 1/14\\ \hat{P}({\sf Chinese}|\overline{c}) &=& (1+1)/(3+6) = 2/9\\ \hat{P}({\sf Tokyo}|\overline{c}) = \hat{P}({\sf Japan}|\overline{c}) &=& (1+1)/(3+6) = 2/9 \end{array}$$

The denominators are (8 + 6) and (3 + 6) because the lengths of  $text_c$  and  $text_{\overline{c}}$  are 8 and 3, respectively, and because the constant *B* in Equation (13.7) is 6 as the vocabulary consists of six terms.

We then get:

$$\begin{split} \hat{P}(c|d_5) &\propto 3/4 \cdot (3/7)^3 \cdot 1/14 \cdot 1/14 \approx 0.0003. \\ \hat{P}(\overline{c}|d_5) &\propto 1/4 \cdot (2/9)^3 \cdot 2/9 \cdot 2/9 \approx 0.0001. \end{split}$$

Thus, the classifier assigns the test document to c = China. The reason for this classification decision is that the three occurrences of the positive indicator Chinese in  $d_5$  outweigh the occurrences of the two negative indicators Japan and Tokyo.

#### Regularized regression

Assume we have:

- $i = 1, 2, \ldots, N$  documents
- Each document *i* is in class  $y_i = 0$  or  $y_i = 1$
- $j = 1, 2, \ldots, J$  unique features
- And x<sub>ij</sub> as the count of feature j in document i

We could build a linear regression model as a classifier, using the values of  $\beta_0$ ,  $\beta_1$ , ...,  $\beta_J$  that minimize:

$$RSS = \sum_{i=1}^{N} \left( y_i - \beta_0 - \sum_{j=1}^{J} \beta_j x_{ij} \right)^2$$

But can we?

- If J > N, OLS does not have a unique solution
- ▶ Even with *N* > *J*, OLS has low bias/high variance (overfitting)

#### Regularized regression

What can we do? Add a penalty for model complexity, such that we now minimize:

$$\sum_{i=1}^{N} \left( y_i - \beta_0 - \sum_{j=1}^{J} \beta_j x_{ij} \right)^2 + \lambda \sum_{j=1}^{J} \beta_j^2 \to \text{ridge regression}$$

or

$$\sum_{i=1}^{N} \left( y_i - \beta_0 - \sum_{j=1}^{J} \beta_j x_{ij} \right)^2 + \lambda \sum_{j=1}^{J} |\beta_j| \rightarrow \text{lasso regression}$$

where  $\lambda$  is the **penalty parameter** (to be estimated)

#### Regularized regression

Why the penalty (shrinkage)?

- Reduces the variance
- Identifies the model if J > N
- Some coefficients become zero (feature selection)

The penalty can take different forms:

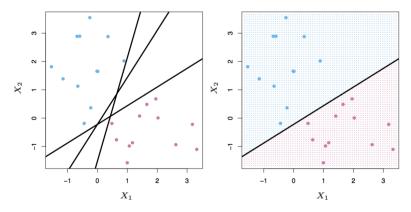
- ▶ Ridge regression:  $\lambda \sum_{j=1}^{J} \beta_j^2$  with  $\lambda > 0$ ; and when  $\lambda = 0$  becomes OLS
- ► Lasso  $\lambda \sum_{j=1}^{J} |\beta_j|$  where some coefficients become zero.
- Elastic Net:  $\lambda_1 \sum_{j=1}^J \beta_j^2 + \lambda_2 \sum_{j=1}^J |\beta_j|$  (best of both worlds?)

How to find best value of  $\lambda$ ? Cross-validation.

Evaluation: regularized regression is easy to interpret, but often outperformed by more complex methods.

#### SVM

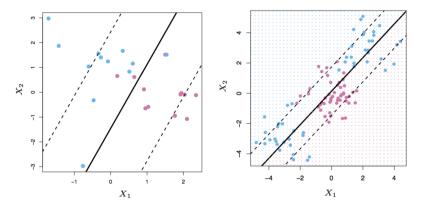
Intuition: finding classification boundary that best separates observations of different classes.



Harder to visualize in more than two dimensions (hyperplanes)

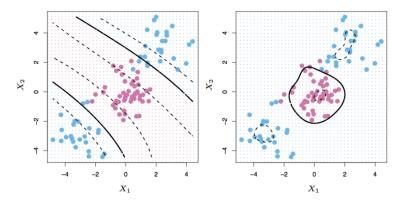
#### Support Vector Machines

With no perfect separation, goal is to minimize distances to marginal points, conditioning on a tuning parameter C that indicates tolerance to errors (controls bias-variance trade-off)



#### SVM

In previous examples, vectors were linear; but we can try different kernels (polynomial, radial):



And of course we can have multiple vectors within same classifier.

#### Ensemble methods

#### Intuition:

- Fit multiple classifiers, different types
- Test how well they perform in test set
- For new observations, produce prediction aggregating predictions of individual classifiers
- How to aggregate predictions?
  - Pick best classifier
  - Average of predicted probabilities
  - Weighted average (weights proportional to classification error)
- Implement in SuperLearner package in R

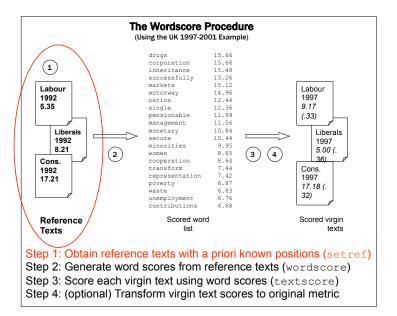
### From Classification to Scaling

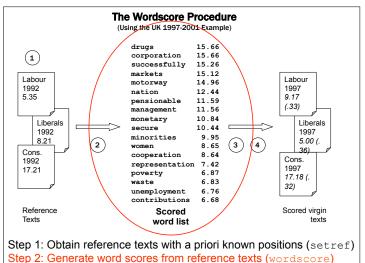
- Machine learning focuses on identifying classes (classification), while social science is typically interested in locating things on latent traits (scaling), e.g.:
  - Policy positions on economic vs social dimension
  - Inter- and intra-party differences
  - Soft news vs hard news
  - Petitioner vs respondent in legal briefs
  - …and any other continuous scale
- But the two methods overlap and can be adapted will demonstrate later using the Naive Bayes classifier
- In fact, the class predictions for a collection of words from NB can be adapted to scaling

#### Supervised scaling methods

Wordscores method (Laver, Benoit & Garry, 2003):

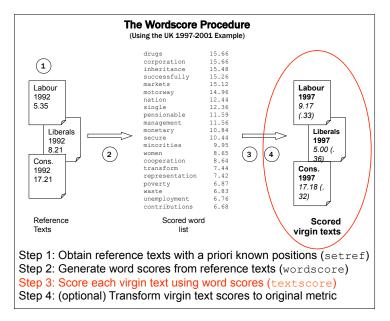
- Two sets of texts
  - Reference texts: texts about which we know something (a scalar dimensional score)
  - Virgin texts: texts about which we know nothing (but whose dimensional score we'd like to know)
- These are analogous to a "training set" and a "test set" in classification
- Basic procedure:
  - 1. Analyze reference texts to obtain word scores
  - 2. Use word scores to score virgin texts

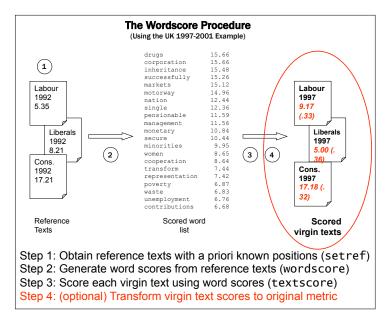




Step 3: Score each virgin text using word scores (textscore)

Step 4: (optional) Transform virgin text scores to original metric





#### Wordscores mathematically: Reference texts

- Start with a set of *I reference* texts, represented by an *I* × *J* document-feature matrix *C<sub>ij</sub>*, where *i* indexes the document and *j* indexes the *J* total word types
- Each text will have an associated "score" a<sub>i</sub>, which is a single number locating this text on a single dimension of difference
  - ▶ This can be on a scale metric, such as 1–20
  - Can use arbitrary endpoints, such as -1, 1
- We normalize the document-feature matrix within each document by converting C<sub>ij</sub> into a relative document-feature matrix (within document), by dividing C<sub>ij</sub> by its word total marginals:

$$F_{ij} = \frac{C_{ij}}{C_{i.}} \tag{2}$$

where  $C_{i.} = \sum_{j=1}^{J} C_{ij}$ 

Wordscores mathematically: Word scores

 Compute an I × J matrix of relative document probabilities P<sub>ij</sub> for each word in each reference text, as

$$P_{ij} = \frac{F_{ij}}{\sum_{i=1}^{I} F_{ij}}$$
(3)

This tells us the probability that given the observation of a specific word j, that we are reading a text of a certain reference document i Wordscores mathematically: Word scores (example)

- Assume we have two reference texts, A and B
- The word "choice" is used 10 times per 1,000 words in Text A and 30 times per 1,000 words in Text B

If we know only that we are reading the word choice in one of the two reference texts, then probability is 0.25 that we are reading Text A, and 0.75 that we are reading Text B

$$P_{A \text{ "choice"}} = \frac{.010}{(.010 + .030)} = 0.25$$
(4)  
$$P_{B \text{ "choice"}} = \frac{.030}{(.010 + .030)} = 0.75$$
(5)

Wordscores mathematically: Word scores

Compute a J-length "score" vector S for each word j as the average of each document i's scores a<sub>i</sub>, weighted by each word's P<sub>ij</sub>:

$$S_j = \sum_{i=1}^{l} a_i P_{ij} \tag{6}$$

- In matrix algebra,  $S_{1\times J} = a_{1\times J} \cdot P_{1\times J}$
- This procedure will yield a single "score" for every word that reflects the balance of the scores of the reference documents, weighted by the relative document frequency of its normalized term frequency

#### Wordscores mathematically: Word scores

- Continuing with our example:
  - ▶ We "know" (from independent sources) that Reference Text A has a position of −1.0, and Reference Text B has a position of +1.0
  - ► The score of the word "choice" is then 0.25(-1.0) + 0.75(1.0) = -0.25 + 0.75 = +0.50

#### Wordscores mathematically: Scoring "virgin" texts

- Here the objective is to obtain a single score for any new text, relative to the reference texts
- We do this by taking the mean of the scores of its words, weighted by their term frequency
- So the score v<sub>k</sub> of a virgin document k consisting of the j word types is:

$$\mathbf{v}_{k} = \sum_{j} (F_{kj} \cdot \mathbf{s}_{j}) \tag{7}$$

where  $F_{kj} = \frac{C_{kj}}{C_{k}}$  as in the reference document relative word frequencies

- Note that new words outside of the set J may appear in the K virgin documents these are simply ignored (because we have no information on their scores)
- Note also that nothing prohibits reference documents from also being scored as virgin documents

Wordscores mathematically: Rescaling raw text scores

- Because of overlapping or non-discriminating words, the raw text scores will be dragged to the interior of the reference scores (we will see this shortly in the results)
- Some procedures can be applied to rescale them, either to a unit normal metric or to a more "natural" metric
- Martin and Vanberg (2008) have proposed alternatives to the LBG (2003) rescaling

#### Computing confidence intervals

- The score  $v_k$  of any text represents a weighted mean
- LBG (2003) used this logic to develop a standard error of this mean using a *weighted variance* of the scores in the virgin text
- Given some assumptions about the scores being fixed (and the words being conditionally independent), this yields approximately normally distributed errors for each v<sub>k</sub>
- ► An alternative would be to bootstrap the textual data prior to constructing C<sub>ij</sub> and C<sub>kj</sub> see Lowe and Benoit (2012)

#### Pros and Cons of the Wordscores approach

- Fully automated technique with minimal human intervention or judgment calls – only with regard to reference text selection
- Language-blind: all we need to know are reference scores
- Could potentially work on texts like this:

#### 

(See http://www.kli.org)

#### Pros and Cons of the Wordscores approach

- Estimates unknown positions on a priori scales hence no inductive scaling with a posteriori interpretation of unknown policy space
- Very dependent on correct identification of:
  - appropriate reference texts
  - appropriate reference scores

#### Suggestions for choosing reference texts

- Texts need to contain information representing a clearly dimensional position
- Dimension must be known a priori. Sources might include:
  - Survey scores or manifesto scores
  - Arbitrarily defined scales (e.g. -1.0 and 1.0)
- Should be as discriminating as possible: extreme texts on the dimension of interest, to provide reference anchors
- Need to be from the same lexical universe as virgin texts
- Should contain lots of words

#### Suggestions for choosing reference values

- Must be "known" through some trusted external source
- ► For any pair of reference values, all scores are simply linear rescalings, so might as well use (-1, 1)
- The "middle point" will not be the midpoint, however, since this will depend on the relative word frequency of the reference documents
- Reference texts if scored as virgin texts will have document scores more extreme than other virgin texts
- With three or more reference values, the mid-point is mapped onto a multi-dimensional simplex. The values now matter but only in relative terms (we are still investigating this fully)