Day 9: Text Scaling II

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When dependent variables are counts

- Many dependent variables of interest may be in the form of counts of discrete events— examples:
 - international wars or conflict events
 - the number of coups d'état
 - deaths
 - word count given an underlying orientation
- ▶ Characteristics: these Y are bounded between $(0, \infty)$ and take on only discrete values $0, 1, 2, \ldots, \infty$
- ▶ Imagine a social system that produces events randomly during a fixed period, and at the end of this period only the total count is observed. For *N* periods, we have *y*₁, *y*₂, ..., *y*_N observed counts

Poisson data model first principles

- 1. The probability that two events occur at precisely the same time is zero
- 2. During each period i, the event rate occurrence λ_i remains constant and is independent of all previous events during the period
 - ▶ note that this implies no *contagion* effects
 - ▶ also known as Markov independence
- 3. Zero events are recorded at the start of the period
- 4. All observation intervals are equal over i

The Poisson distribution

$$f_{Poisson}(y_i|\lambda) = \begin{cases} rac{e^{-\lambda}\lambda^{y_i}}{y_i!} & orall \ \lambda > 0 \ ext{and} \ y_i = 0, 1, 2, \dots \\ 0 & ext{otherwise} \end{cases}$$
 $Pr(Y|\lambda) = \prod_{i=1}^n rac{e^{-\lambda}\lambda^{y_i}}{y_i!}$ $\lambda = e^{X_i\beta}$ $E(y_i) = \lambda$ $Var(y_i) = \lambda$

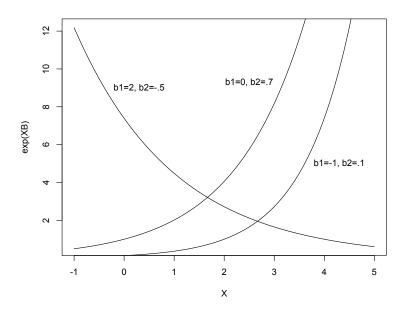
Systematic component

- $\lambda_i > 0$ is only bounded from below (unlike π_i)
- This implies that the effect cannot be linear
- Hence for the functional form we will use an exponential transformation

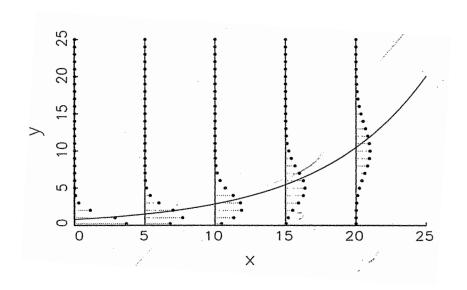
$$\mathsf{E}(Y_i) = \lambda_i = e^{X_i\beta}$$

 Other possibilities exist, but this is by far the most common – indeed almost universally used – functional form for event count models

Exponential link function



Exponential link function



Likelihood for Poisson

$$L(\lambda|y) = \prod_{i=1}^{N} \frac{e^{-\lambda_{i}} \lambda_{i}^{y_{i}}}{y_{i}!}$$

$$\ln L(\lambda|y) = \sum_{i=1}^{N} \ln \left[\frac{e^{-\lambda_{i}} \lambda_{i}^{y_{i}}}{y_{i}!} \right]$$

$$= \sum_{i=1}^{N} \left\{ \ln e^{-\lambda_{i}} + \ln(\lambda_{i}^{y_{i}}) + \ln\left(\frac{1}{y_{i}!}\right) \right\}$$

$$= \sum_{i=1}^{N} \left\{ -\lambda_{i} + y_{i} \ln(\lambda_{i}) - \ln(y_{i}!) \right\}$$

$$= \sum_{i=1}^{N} \left\{ -e^{X_{i}\beta} + y_{i} \ln e^{X_{i}\beta} - \ln y_{i}! \right\}$$

$$\propto \sum_{i=1}^{N} \left\{ -e^{X_{i}\beta} + y_{i} X_{i}\beta - dropped \right\}$$

$$\ln L(\beta|y) \propto \sum_{i=1}^{N} \left\{ X_{i}\beta y_{i} - e^{X_{i}\beta} \right\}$$

Models for continuous θ

Background: Spatial politics Methods

- Wordscores
- Wordfish

Document scaling is for continuous θ

Some spatial theory

Spatial theories of national voting assumes that

- ▶ Voters and politicians/parties have *preferred positions* 'ideal points' on ideological dimensions or policy spaces
- ► Voters support the politician/prty with the ideal point *nearest* their own
- Politicians/parties position themselves to maximize their vote share

Some spatial theory

Spatial theories of parliamentary voting assume that

- ► Each vote is a decision between *two* policy outcomes
- Each outcomes has a position on an ideological dimension or a policy space
- ▶ Voters choose the outcome *nearest* to their own ideal point

Unobserved ideal points / policy positions: θ Voting 'reveals' θ (sometimes)

Spatial utility models

Measurement models for votes (Jackman, 2001; Clinton et al. 2004) connect voting choices to personal utilities and ideal points Parliamentary voting example: Ted Kennedy on the 'Federal Marriage Amendment'

$$U(\pi_{\text{yes}}) = -\|\theta - \pi_{\text{yes}}\|^2 + \epsilon_{\text{yes}}$$

$$U(\pi_{\text{no}}) = -\|\theta - \pi_{\text{no}}\|^2 + \epsilon_{\text{no}}$$

- $\triangleright \theta$ is Kennedy's ideal point
- \blacktriangleright π_{yes} is the policy outcome of the FMA passing (vote yes)
- \blacktriangleright π_{no} is the policy outcome of the FMA failing (vote no)

Votes 'yes' when $U(\pi_{\text{yes}}) > U(\pi_{\text{no}})$

Spatial utility models and voting

What is the probability that Ted votes yes?

$$\begin{split} P(\text{Ted votes yes}) &= P(U(\pi_{\text{yes}}) > U(\pi_{\text{no}})) \\ &= P(\epsilon_{\text{no}} - \epsilon_{\text{yes}} < \|\theta - \pi_{\text{no}}\|^2 - \|\theta - \pi_{\text{yes}}\|^2) \\ &= P(\epsilon_{\text{no}} - \epsilon_{\text{yes}} < 2(\pi_{\text{yes}} - \pi_{\text{no}})\theta + \pi_{\text{no}}^2 - \pi_{\text{yes}}^2) \end{split}$$

 $logit P(Ted votes yes) = \beta \theta + \alpha$

Only the 'cut point' or separating hyperplane between $\pi_{\rm yes}$ and $\pi_{\rm no}$ matters

This is logistic regression model with explanatory variable heta

Spatial voting models

This is a simple measurement model There is some distribution of ideal points in the population (the legislature)

$$P(\theta) = Normal(0,1)$$

Votes are conditionally independent given ideal point

$$P(\mathsf{vote}_1, \dots, \mathsf{vote}_K \mid \theta) = \prod_j P(\mathsf{vote}_j \mid \theta)$$

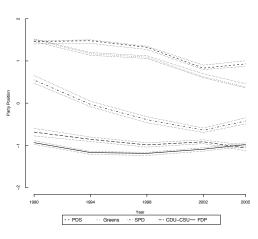
Probability of voting yes is monotonic in the *difference* between policy outcomes

$$P(\text{yes}) = \text{Logit}^{-1}(\beta\theta + \alpha)$$

Poisson scaling models for text

Poisson scaling models for text (aka "wordfish") is a statistical model for inferring policy positions θ from words

Left-Right Positions in Germany, 1990–2005 including 95% confidence intervals



As measurement model

Assumptions about $P(W_1 \dots W_V \mid \theta)$

$$\log E(W_i \mid \theta_j) = \alpha_j + \psi_i + \beta_i \theta_j$$

- $ightharpoonup lpha_j$ is a constant term controlling for document length (hence it's associated with the party or politician)
- ▶ The sign of β_i represents the ideological direction of W_i
- ▶ The magnitude of β_i represents the sensitivity of the word to ideological differences among speakers or parties
- \blacktriangleright Ψ is a constant term for the word (larger for high frequency words).

The Poisson scaling "wordfish" model

Data:

 $ightharpoonup
m{Y}$ is N (speaker) imes V (word) term document matrix $V\gg N$

Model:

$$P(Y_i \mid \theta) = \prod_{j=1}^{V} P(Y_{ij} \mid \theta_i)$$

$$Y_{ij} \sim Poisson(\lambda_{ij})$$

$$\log \lambda_{ij} = (g +) \alpha_i + \theta_i \beta_j + \psi_j$$
(POIS)

Estimation:

▶ Easy to fit for large V (V Poisson regressions with α offsets)

Model components and notation

Element	Meaning
i	indexes the targets of interest (political actors)
Ν	number of political actors
j	indexes word types
V	total number of word types
$ heta_i$	the unobservable political position of actor i
$eta_{m{j}}$	word parameters on θ – the "ideological" direction of word j
$\psi_j \ lpha_i$	word "fixed effect" (function of the frequency of word j) actor "fixed effects" (a function of (log) document length to allow estimation in Poisson of an essentially multinomial process)

How to estimate this model

Maximimum likelihood estimation using (a form of) Expectation Maximization:

- ▶ If we knew Ψ and β (the word parameters) then we have a Poisson regression model
- ▶ If we knew α and θ (the party / politician / document parameters) then we have a Poisson regression model too!
- So we alternate them and hope to converge to reasonable estimates for both

The iterative (conditional) maximum likelihood estimation

Start by *guessing* the parameters

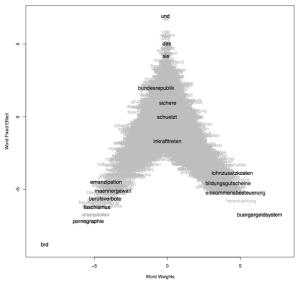
Algorithm:

- Assume the current party parameters are correct and fit as a Poisson regression model
- Assume the current word parameters are correct and fit as a Poisson regression model
- Normalize θ s to mean 0 and variance 1

Repeat

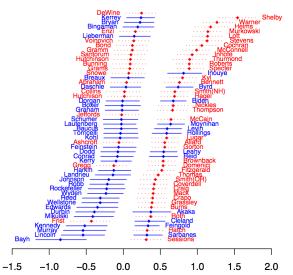
Frequency and informativeness

 Ψ and β (frequency and informativeness) tend to trade-off. . .



Plotting θ

Plotting θ (the ideal points) gives estimated positions. Here is Monroe and Maeda's (essentially identical) model of legislator positions:



Wordscores and Wordfish as measurement models

Wordfish assumes that

$$P(\theta) = Normal(0,1)$$

and that $P(W_i \mid \theta)$ depends on

- lacktriangle Word parameters: eta and ψ
- **Document** / party / politician parameters: θ and α

Wordscores and Wordfish as measurement models

Wordfish estimates of θ control for

- different document lengths (α)
- ▶ different word frequencies (ψ) different levels of ideological relevance of words (β) .

But there are no wordscores!

Words do not have an ideological position themselves, only a sensitivity to the speaker's ideological position

Wordscores and Wordfish as measurement models

Wordscores makes no explicit assumption about $P(\theta)$ except that it is continuous

We infer that $P(W_i \mid \theta)$ depends on

- \blacktriangleright Wordscores: π
- Document scores: θ

Hence θ estimates do *not* control for

- different word frequencies
- different levels of ideological relevance of words

Dimensions

- ▶ How to interpret $\hat{\theta}$ s substantively?
- One option is to regress them other known descriptive variables
- ► Example European Parliament speeches (Proksch and Slapin)
 - Inferred ideal points seem to reflect party positions on EU integration better than national left-right party placements

Identification

The scale and direction of θ is undetermined — like most models with latent variables

To identify the model in Wordfish

- Fix one α to zero to specify the left-right direction (Wordfish option 1)
- Fix the $\hat{\theta}$ s to mean 0 and variance 1 to specify the scale (Wordfish option 2)
- Fix two $\hat{\theta}$ s to specify the direction and scale (Wordfish option 3 and Wordscores)

Implication: Fixing two reference scores does not specify the policy domain, it just identifies the model!

Dimensions

How infer more than one dimension?

This is two questions:

- ► How to get two dimensions (for all policy areas) at the same time?
- ▶ How to get one dimension for each policy area?

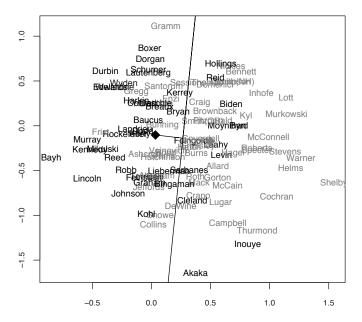
Dimensions

To get one dimension for each policy area, split up the document by hand and use the subparts as documents (the Slapin and Proksch method)

There is currently *no* implementation of Wordscores or Wordfish that extracts two or more dimensions at once

▶ But since Wordfish is a type of factor analysis model, there is no reason in principle why it could not

The hazards of ex-post interpretation illustrated



"Features" of the parametric scaling approach

- Standard (statistical) inference about parameters
- Uncertainty accounting for parameters
- Distributional assumptions are laid nakedly bare for inspection
 - conditional independence
 - ▶ stochastic process (e.g. $E(Y_{ij}) = Var(Y_{ij}) = \lambda_{ij}$)
- ► Permits hierarchical reparameterization (to add covariates)
- Prediction: in particular, out of sample prediction

Problems laid bare I: Conditional (non-)independence

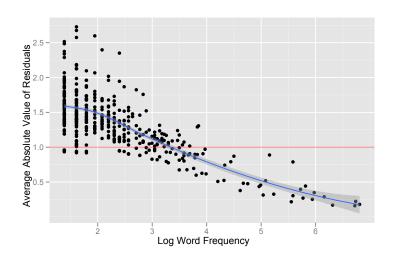
- Words occur in order
 In occur words order.
 Occur order words in.
 "No more training do you require. Already know you that which you need." (Yoda)
- ► Words occur in combinations "carbon tax" / "income tax" / "inhertiance tax" / "capital gains tax" /" bank tax"
- Sentences (and topics) occur in sequence (extreme serial correlation)
- Style may mean means we are likely to use synonyms very probable. In fact it's very distinctly possible, to be expected, odds-on, plausible, imaginable; expected, anticipated, predictable, predicted, foreseeable.)
- ▶ Rhetoric may lead to repetition. ("Yes we can!") anaphora

Problems laid bare II: Parametric (stochastic) model

- ▶ Poisson assumes $Var(Y_{ij}) = E(Y_{ij}) = \lambda_{ij}$
- ► For many reasons, we are likely to encounter overdispersion or underdispersion
 - overdispersion when "informative" words tend to cluster together
 - underdispersion could (possibly) occur when words of high frequency are uninformative and have relatively low between-text variation (once length is considered)
- ► This should be a word-level parameter

Overdispersion in German manifesto data

(from Slapin and Proksch 2008)



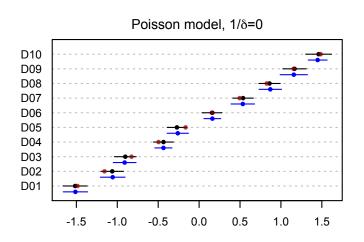
How to account for uncertainty?

- ▶ Don't. (SVD-like methods, e.g. correspondence analysis)
- Analytical derivatives
- Parametric bootstrapping (Slapin and Proksch, Lewis and Poole)
- Non-parametric bootstrapping
- (and yes of course) Posterior sampling from MCMC

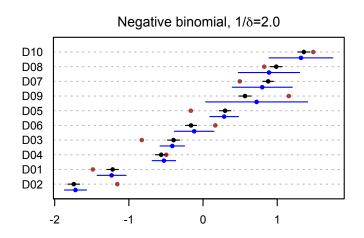
Steps forward

- ▶ Diagnose (and ultimately treat) the issue of whether a separate variance parameter is needed
- ▶ Diagnose (and treat) violations of conditional independence
- ▶ Explore non-parametric methods to estimate uncertainty

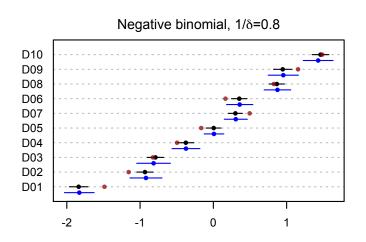
Diagnosis I: Estimations on simulated texts



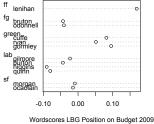
Diagnosis I: Estimations on simulated texts

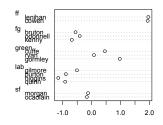


Diagnosis I: Estimations on simulated texts

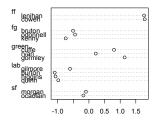


Diagnosis 2: Irish Budget debate of 2009



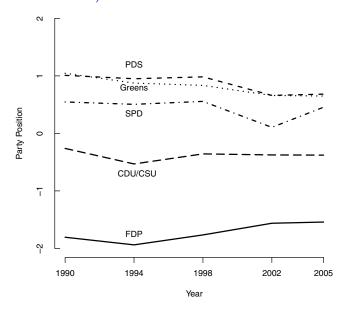


Normalized CA Position on Budget 2009

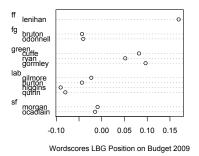


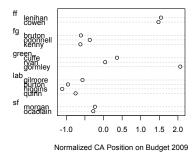
Classic Wordfish Position on Budget 2009

Diagnosis 3: German party manifestos (economic sections) (Slapin and Proksch 2008)



Diagnosis 4: What happens if we include irrelevant text?





Diagnosis 4: What happens if we include irrelevant text?



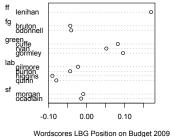
John Gormley: leader of the Green Party and Minister for the Environment, Heritage and Local Government

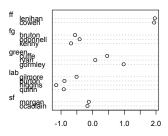
"As leader of the Green Party I want to take this opportunity to set out my party's position on budget 2010..."

[772 words later]

"I will now comment on some specific aspects of my Department's Estimate. I will concentrate on the principal sectors within the Department's very broad remit ..."

Diagnosis 4: Without irrelevant text





Normalized CA Position on Budget 2009

The Way Forward

- Parametric Poisson model with variance parameter ("negative binomial" with parameter for over- or under-dispersion at the word level, could use CML
- Block Bootstrap resampling schemes
 - text unit blocks (sentences, paragraphs)
 - fixed length blocks
 - variable length blocks
 - could be overlapping or adjacent
- More detailed investigation of feasible methods for characterizing fundamental uncertainty from non-parametric scaling models (CA and others based on SVD)

The Negative Binomial model

Generalize the Poisson model to:

$$f_{nb}(y_i|\lambda_i,\sigma^2)$$
 where :

- $ightharpoonup \sigma^2$ is the variability (a new parameter v. Poisson)
- \triangleright λ_i is the expected number of events for i
- λ is the average of individual λ_i s
- ▶ Here we have dropped Poisson assumption that $\lambda_i = \lambda \ \forall \ i$
- New assumption: Assume that λ_i is a random variable following a *gamma* distribution (takes on only non-negative numbers)
- ▶ For the NB model, $Var(Y_i) = \lambda_i \sigma^2$ for $\lambda_i > 0$ and $\sigma^2 > 0$

The Negative Binomial model cont.

- ▶ For the NB model, $Var(Y_i) = \lambda_i \sigma^2$ for $\lambda_i > 0$ and $\sigma^2 > 0$
- ▶ How to interpret σ^2 in the negative binomial
 - when $\sigma^2 = 1.0$, negative binomial \equiv Poisson
 - when $\sigma^2 > 1$, then it means there is overdispersion in Y_i caused by correlated events, or heterogenous λ_i
 - when $\sigma^2 < 1$ it means something strange is going on
- ▶ When $\sigma^2 \neq 1$, then Poisson results will be inefficient and standard errors inconsistent
- ▶ Functional form: same as Poisson

$$E(y_i) = \lambda$$

▶ Variance of λ is now:

$$Var(y_i) = \lambda_i \sigma^2 = e^{X_i \beta} \sigma^2$$